



# Algorithm Engineering für grundlegende Datenstrukturen und Algorithmen

**Peter Sanders**

Was sind die **schnellsten implementierten Algorithmen**

für das  $1 \times 1$  der Algorithmik:

Listen, Sortieren, Prioritätslisten, Sortierte Listen,

Graphenalgorithmen? + Exkurse in die ITI-Forschung: z.B.

Routenplanung



# Nützliche Vorkenntnisse

- Informatik I/II
- Algorithmentechnik (gleichzeitig hören vermutlich OK)
- etwa Rechnerarchitektur (oder Ct lesen ;-)
- passive Kenntnisse von C/C++

Vertiefungsgebiet: Algorithmik



# Material

- Folien
- wissenschaftliche Aufsätze. Siehe Vorlesungshomepage
- Basiskenntnisse: Algorithmenlehrbücher, z.B. Cormen Leiserson Rivest???, Mehlhorn, Sedgewick, sowie ein Manuskript zu einem neuen Lehrbuch
- Mehlhorn Näher: The LEDA Platform of Combinatorial and Geometric Computing. Gut für die fortgeschrittenen Papiere.



# Überblick

- Was ist Algorithm Engineering, Modelle, ...
- Exkurs: Routenplanung
- Erste Schritte: Arrays, verkettete Listen, Stacks, FIFOs,...
- Sortieren rauf und runter
- Prioritätslisten
- Sortierte Listen
- Minimale Spannbäume
- Volltextindices
- Kürzeste Wege
- Ausgewählte fortgeschrittene Algorithmen, z.B. maximale Flüsse

Methodik: in Exkursen



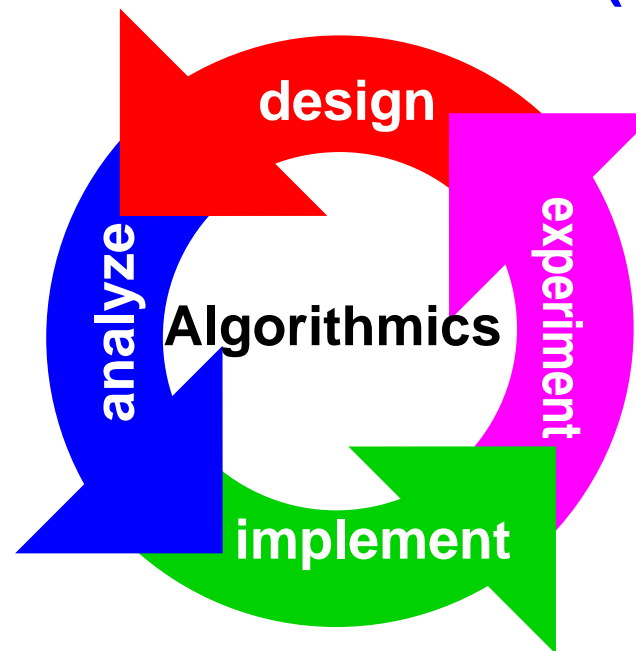
# Algorithm Engineering

## An Attempt at a Definition

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Joint work with:

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More: DFG Focus Program [www.algorithm-engineering.de](http://www.algorithm-engineering.de)



# Overview

## A detailed definition

- in general
- simple** examples, mostly **external MSTs**

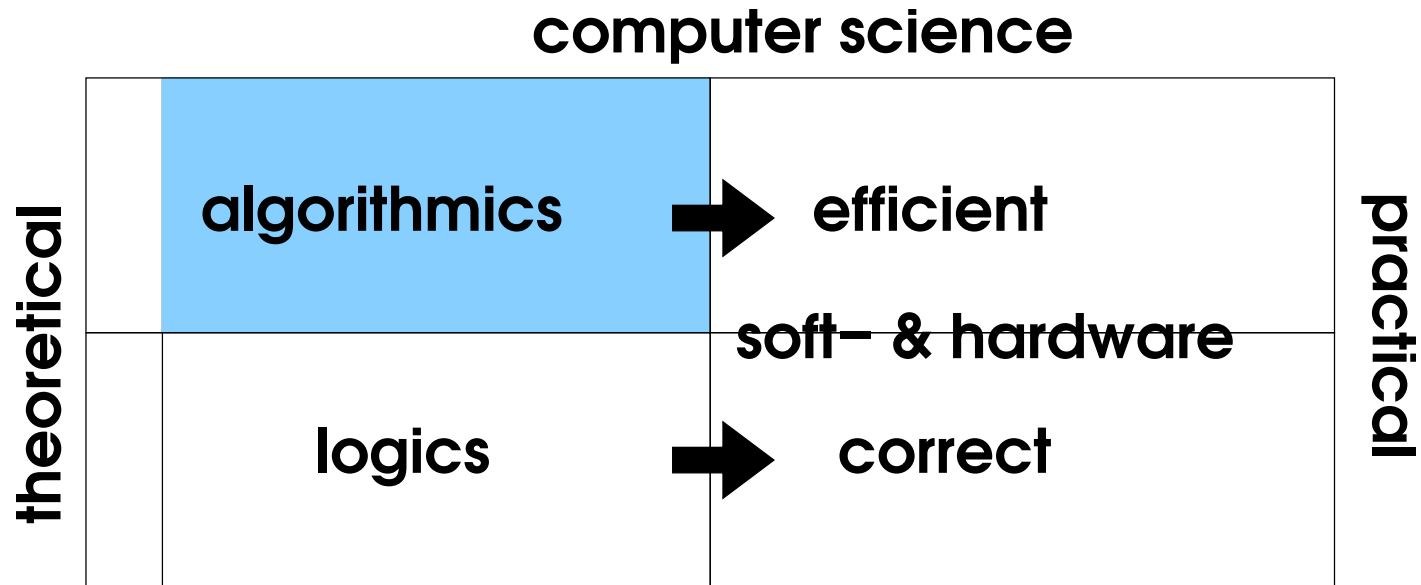
## More algorithm engineering in my group

- The **basic toolbox**
- Various **applications**



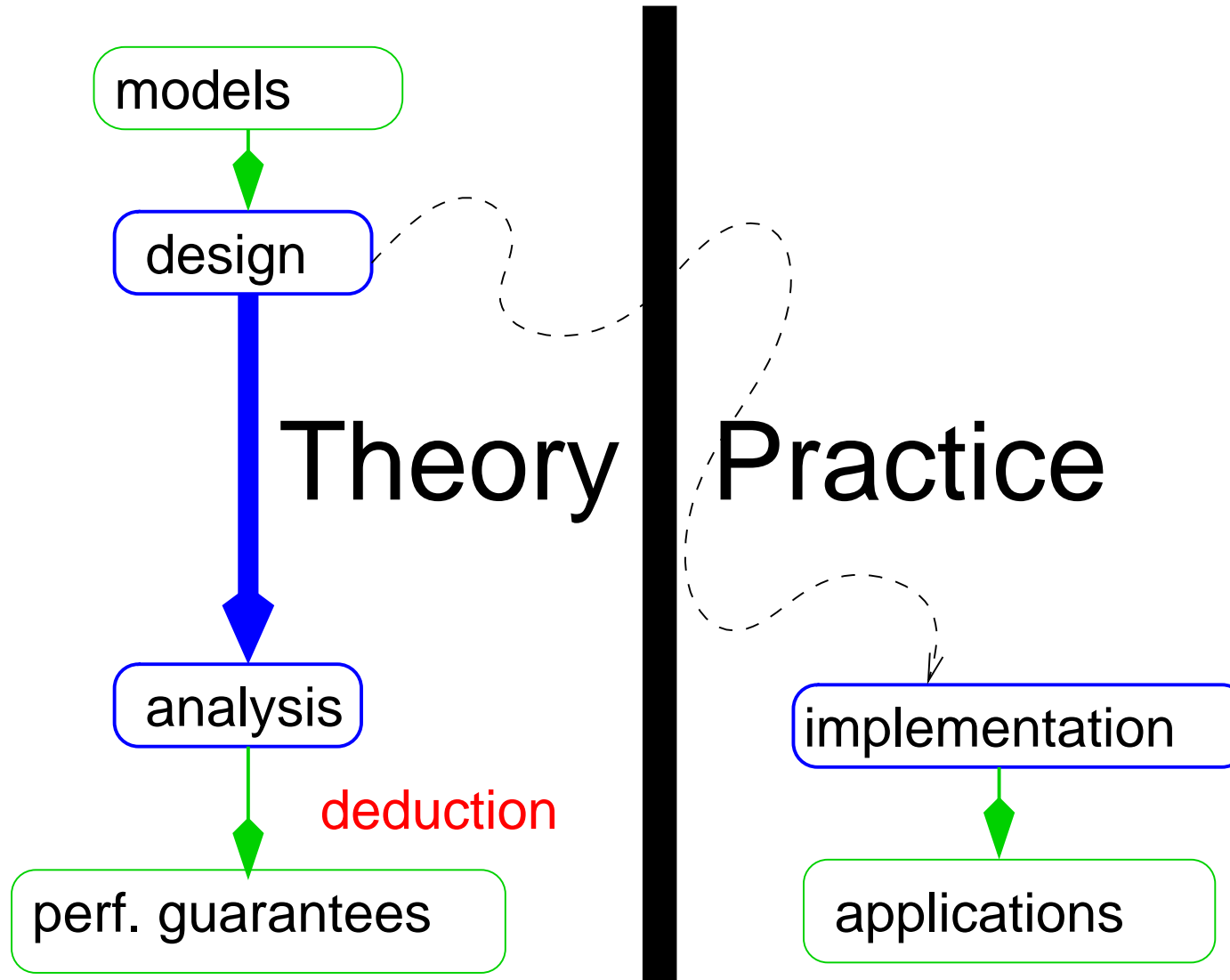
# Algorithmics

= the **systematic** design of efficient software and hardware





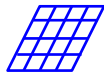

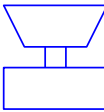


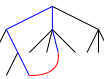


# (Caricatured) Traditional View: Algorithm Theory





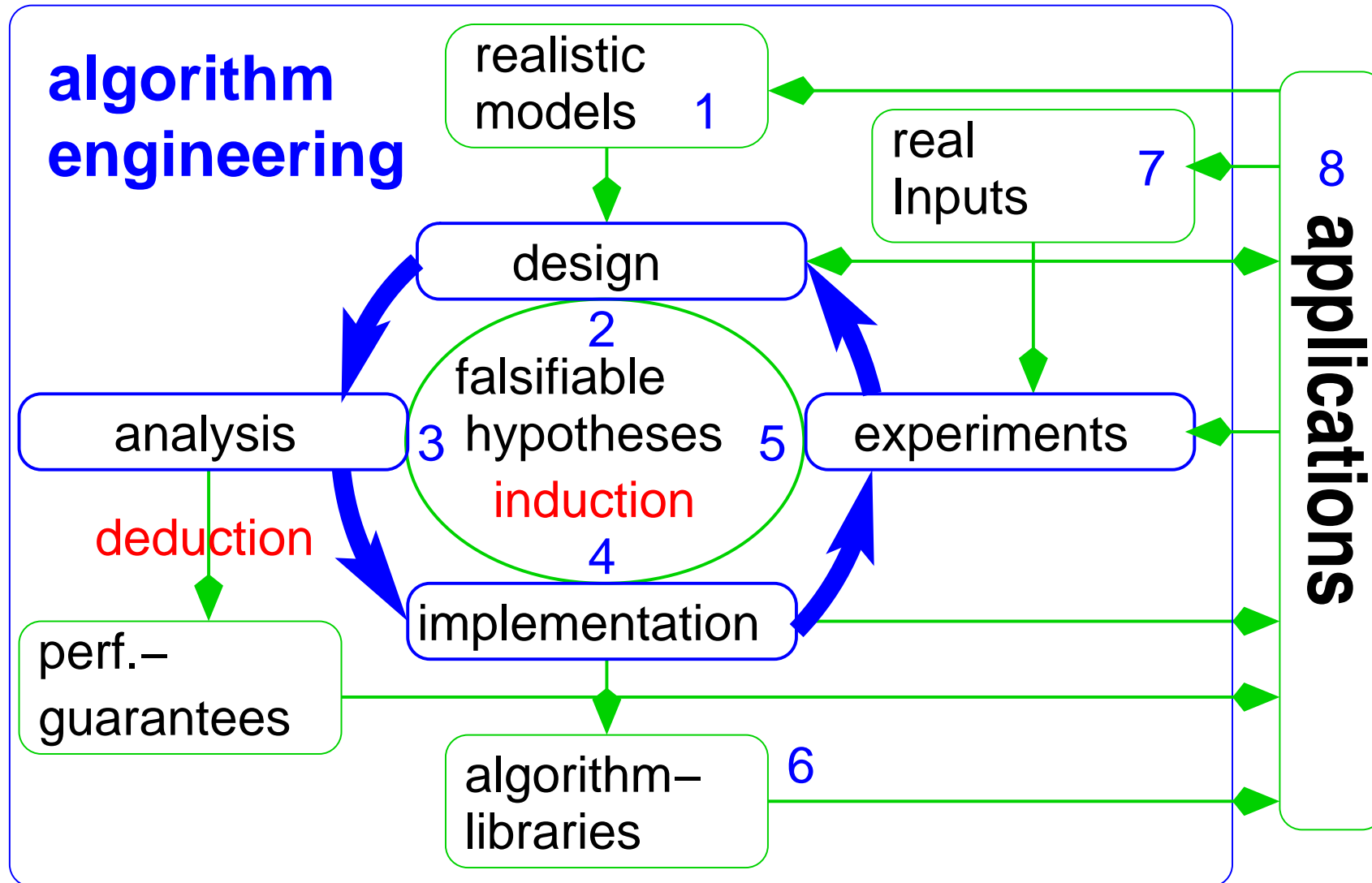


# Gaps Between Theory & Practice

Theory	↔	Practice
simple 	<b>appl. model</b>	 complex
simple 	<b>machine model</b>	 real
complex 	<b>algorithms</b>	<span style="border: 1px solid blue; padding: 2px;">FOR</span> simple
advanced 	<b>data structures</b>	 arrays,...
worst case <span style="border: 1px solid blue; padding: 2px;">max</span>	<b>complexity measure</b>	 inputs
asympt. <span style="border: 1px solid blue; padding: 2px;"><math>O(\cdot)</math></span>	<b>efficiency</b>	<span style="border: 1px solid blue; padding: 2px;">42%</span> constant factors



# Algorithmics as Algorithm Engineering





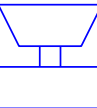



# Goals

- bridge gaps** between theory and practice
- accelerate **transfer** of algorithmic results into **applications**
- keep the advantages of theoretical treatment:  
**generality** of solutions and  
**reliability, predictability** from performance guarantees



# 1: Realistic Models

Theory	$\longleftrightarrow$	Practice
simple 	<b>appl. model</b>	 complex
simple 	<b>machine model</b>	 real

- Careful refinements
- Try to preserve (partial) analyzability / simple results

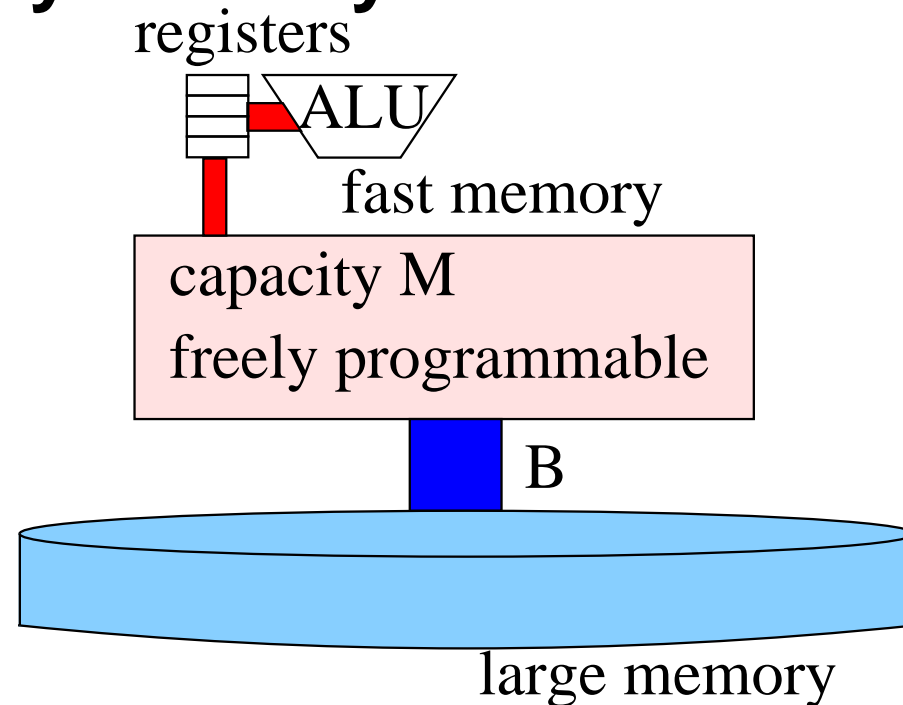




# Example: The Secondary Memory Model

$M$ : Fast memory of size  $M$

$B$ : Block size (?)



**Analysis: count block accesses (I/Os)**

e.g. Sorting in  $\text{sort}(n) := \frac{2n}{DB} \left( 1 + \left\lceil \log_{M/B} \frac{n}{M} \right\rceil \right)$  I/Os

Variants:  $D$  parallel disks, cache oblivious ( $M, B$  unknown)

Challenge: parallel, hierarchical memory model



## 2: Design

of algorithms that work well in **practice**

- simplicity**
- reuse**
- constant** factors
- exploit **easy** instances



## 3: Analysis

- Constant factors** matter
- Beyond worst case** analysis
- Practical algorithms** might be difficult to analyze  
(randomization, meta heuristics, . . .)



# 4: Implementation

sanity check for algorithms !

## Challenges

Semantic gaps:

Abstract algorithm

↔

C++...

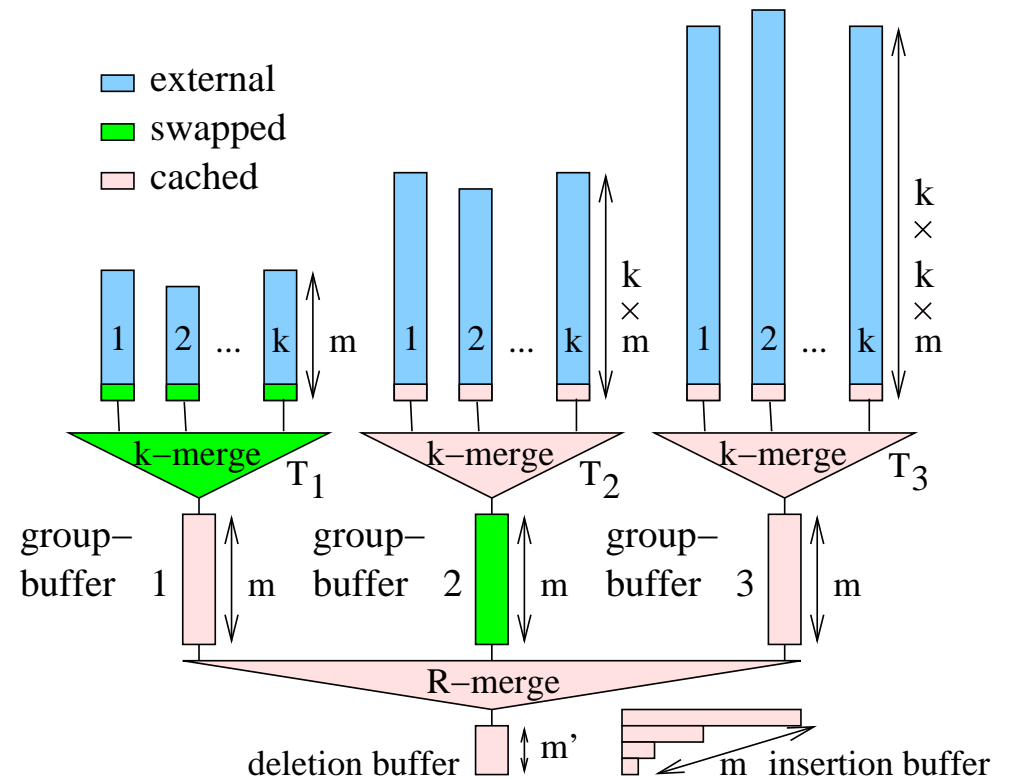
↔

hardware

Small constant factors:

compare highly tuned competitors,

## Sequence Heap External Priority Queues







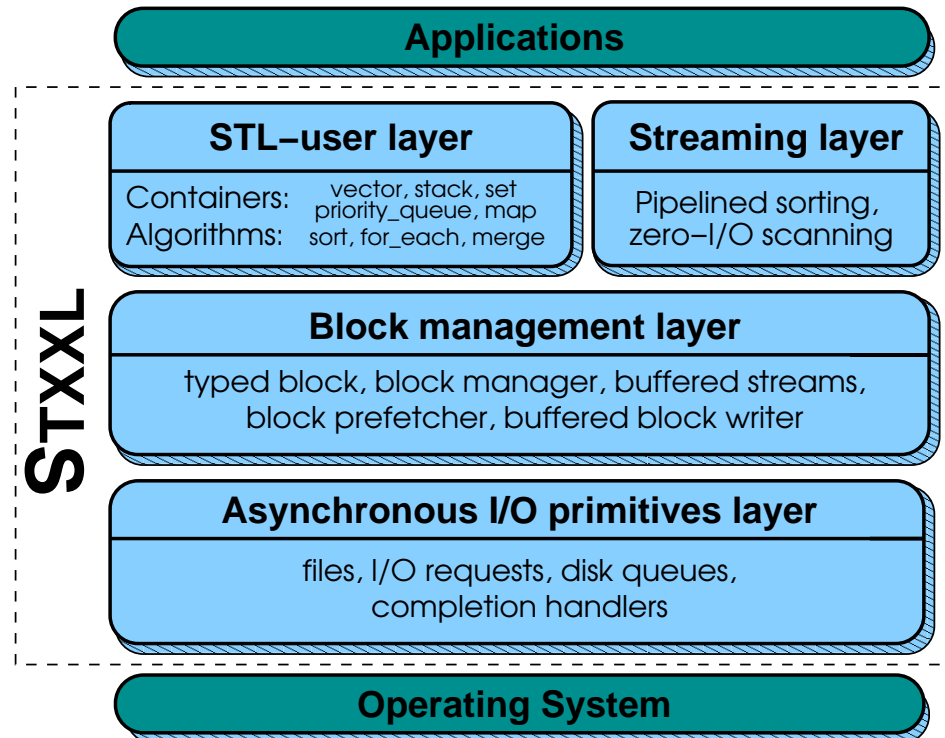
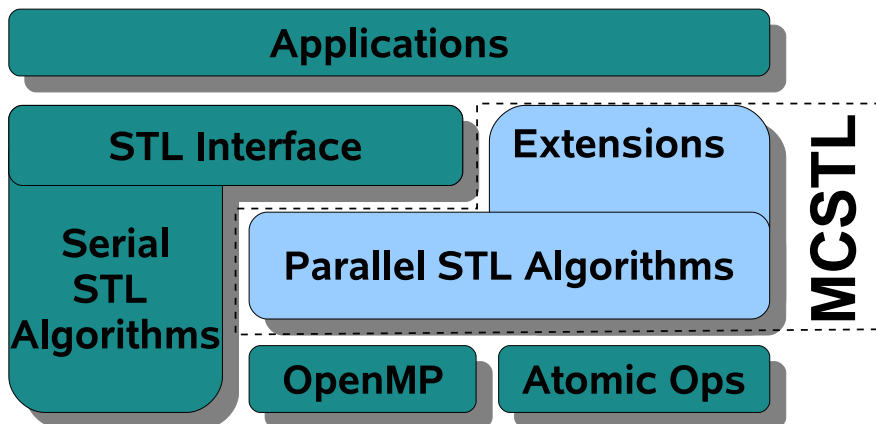
## 5: Experiments

- sometimes a good **surrogate for analysis**
- too much** rather than too little **output data**
- reproducibility** (10 years!)
- software engineering**



# 6: Algorithm Libraries — Challenges

- software engineering, e.g. CGAL
- standardization, e.g. java.util, C++ STL and BOOST
- performance ↔ generality ↔ simplicity
- applications are a priori unknown
- result checking, verification

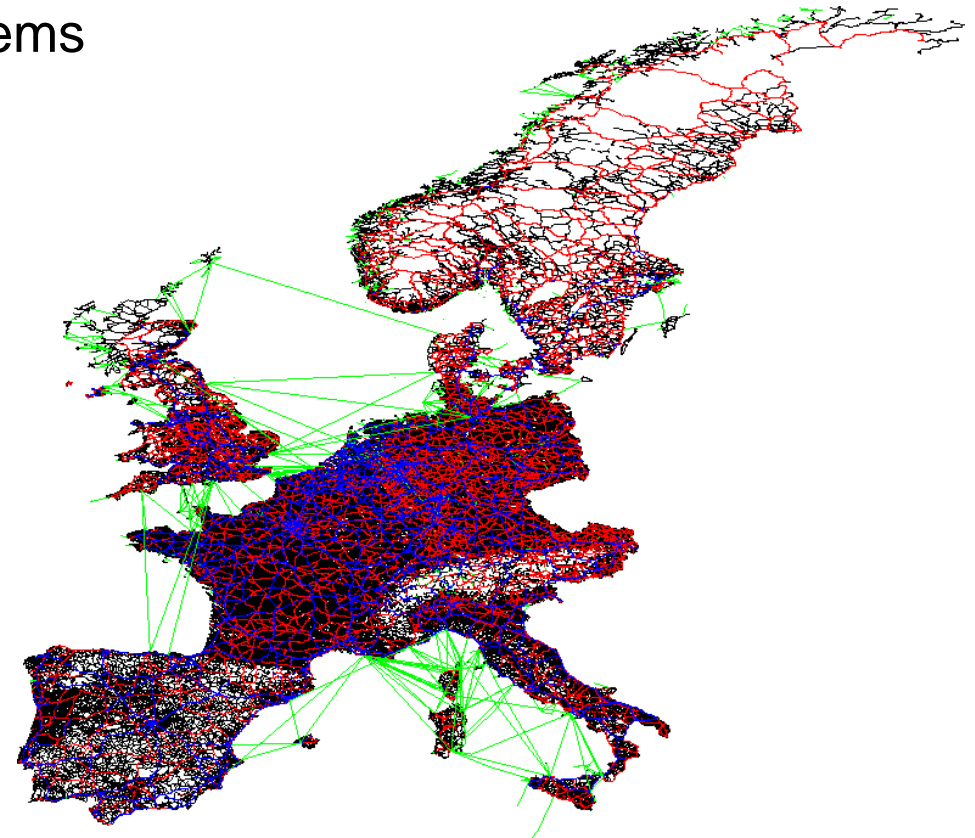




## 7: Problem Instances

Benchmark instances for **NP-hard** problems

- TSP
- Steiner-Tree
- SAT
- set covering
- graph partitioning
- ...



have proved essential for development of practical algorithms

**Strange:** much less real world instances for **polynomial problems**

(**MST**, **shortest path**, max flow, matching...)



## **8: Applications that “Change the World”**

Algorithmics has the potential to SHAPE applications  
(not just the other way round)

[G. Myers]

**Bioinformatics:** sequencing, proteomics, phylogenetic trees,...



**Information Retrieval:** Searching, ranking,...

**Traffic Planning:** navigation, flow optimization,  
adaptive toll, disruption management

**Geographic Information Systems:** agriculture, environmental protection,  
disaster management, tourism,...

**Communication Networks:** mobile, P2P, grid, selfish users,...



## Conclusion:

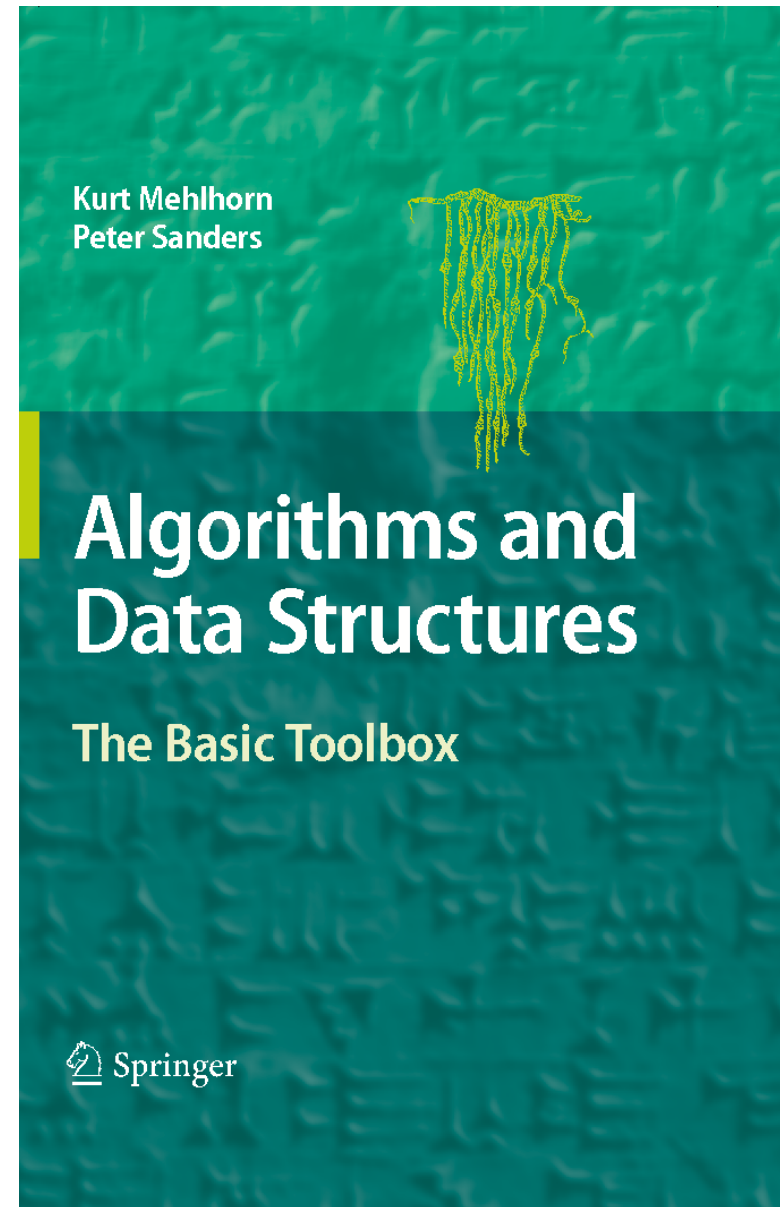
### Algorithm Engineering $\leftrightarrow$ Algorithm Theory

- algorithm engineering** is a wider view on **algorithmics**  
(but no revolution. None of the ingredients is really new)
- rich **methodology**
- better coupling to **applications**
- experimental algorithmics**  $\ll$  algorithm engineering
- algorithm theory**  $\subset$  algorithm engineering
- sometimes **different theoretical questions**
- algorithm theory may still yield the **strongest, deepest and most persistent** results **within algorithm engineering**



# Fundamental Algorithms

- lists, array, stacks, queues
- sorting**
- priority queues
- sorted lists / search trees
- hash tables
- graph algorithms**
  - graph traversal (DFS, BFS)
  - **shortest paths**
  - **minimal spanning trees**
  - flow problems
- strings**





# Application Areas

- combinatorial optimization
  - parallel computing
    - C++ Standard Library for Multicore
    - MPI communication primitives
    - load balancing
  - external memory computations
  - scalable (virtual) storage servers
  - information retrieval      → Cooperation with SAP TREX group
- here  
worked on



# Interactions with other (Sub)disciplines

