

Accelerating SAT Based Planning with Incremental SAT Solving

1. What is Planning?

- World state: instantiation of multi valued state variables
- Actions:
 - require certain values of state variables to be used
 - change values of state variables by their effects
- Objective:**
 - Given a set of actions
 - Given an initial state (start) and goal conditions
 - Find a plan (sequence of actions to get from start to goal)

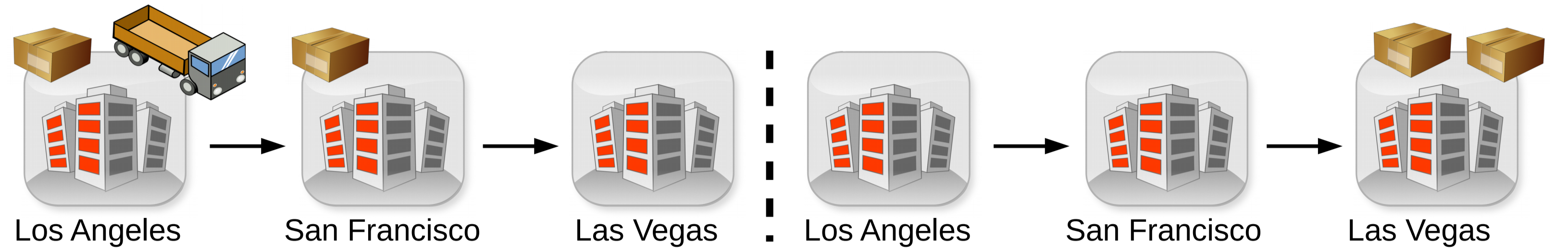
3. Finding Plans with Satisfiability Solvers

- Create F_k which is satisfiable only if plan of size k exists
- Many encoding schemes for F_k exist
 - use abstract view, such that all can be used:
 - initial clauses I:
 - satisfied in the initial state
 - goal clauses G:
 - satisfied in the goal state
 - transition clauses T:
 - satisfied at each pair of consecutive states
- Solve F_1, F_2, \dots until a satisfiable formula F_n is reached
- Use the solution of F_n to construct a plan

Goal to Init or Init to Goal?

BOTH!

2. Example: delivering 2 packages to Las Vegas



State Variables and their domains:

- Truck location T , $\text{dom}(T) = \{LA, SF, LV\}$
- Package locations P and Q
 $\text{dom}(P) = \text{dom}(Q) = \{LA, SF, LV, Tr\}$

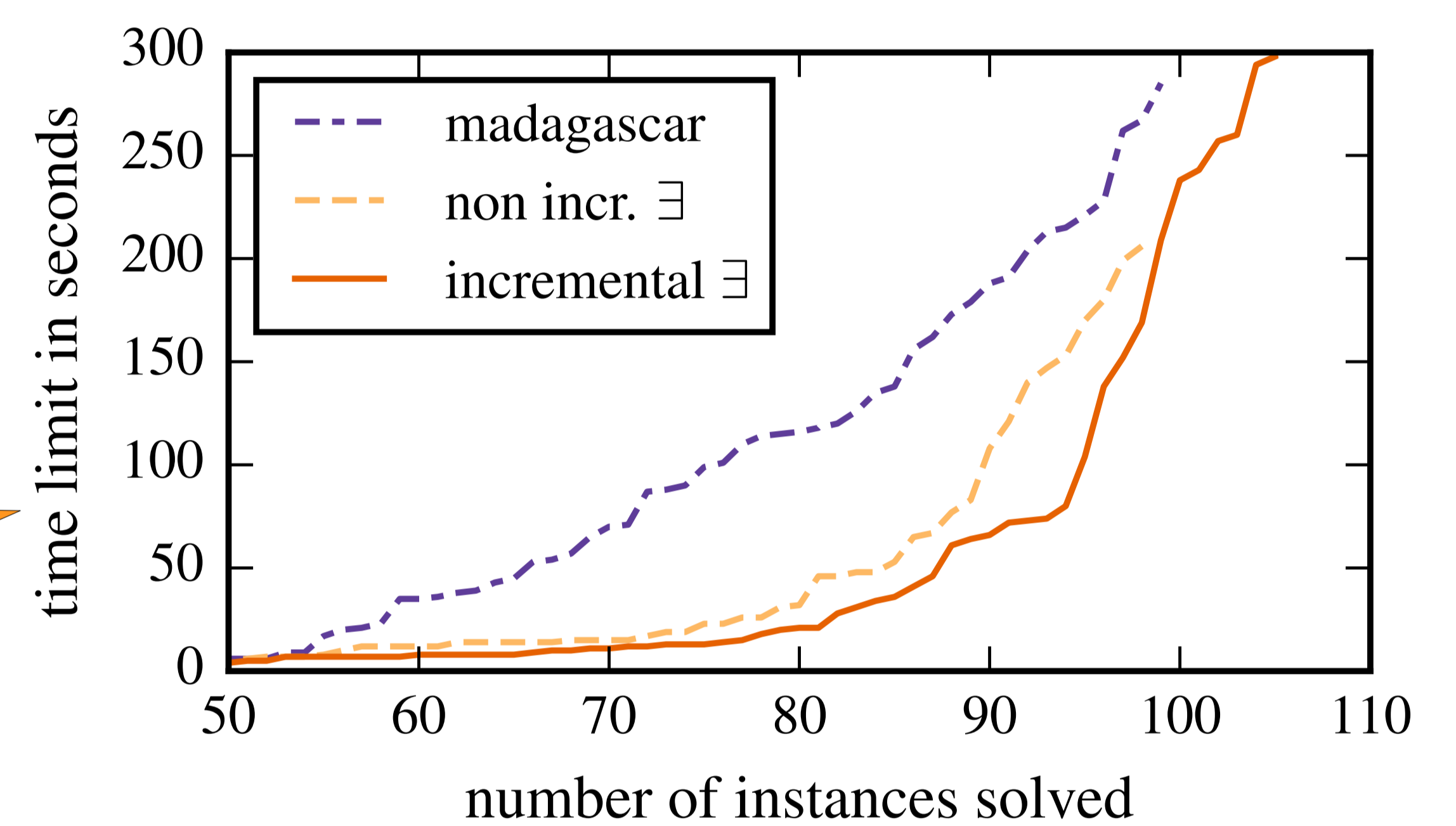
Initial State: $T=LA, P=LA, Q=SF$

Goal Conditions: $P=LV, Q=LV$

Plan: $\text{loadP}(LA), \text{move}(LA,SF), \text{loadQ}(SF), \text{move}(SF,LV), \text{dropP}(LV), \text{dropQ}(LV)$

Actions:

- $\text{move}(x,y)=[\text{prec: } \{T=x\}, \text{eff: } \{T=y\}]$
 - $\text{loadP}(x)=[\text{prec: } \{T=x, P=x\}, \text{eff: } \{P=Tr\}]$
 - $\text{loadQ}(x)=[\text{prec: } \{T=x, Q=x\}, \text{eff: } \{Q=Tr\}]$
 - $\text{dropP}(x)=[\text{prec: } \{T=x, P=Tr\}, \text{eff: } \{P=x\}]$
 - $\text{dropQ}(x)=[\text{prec: } \{T=x, Q=Tr\}, \text{eff: } \{Q=x\}]$
- Where x,y are LA, SF, and LV



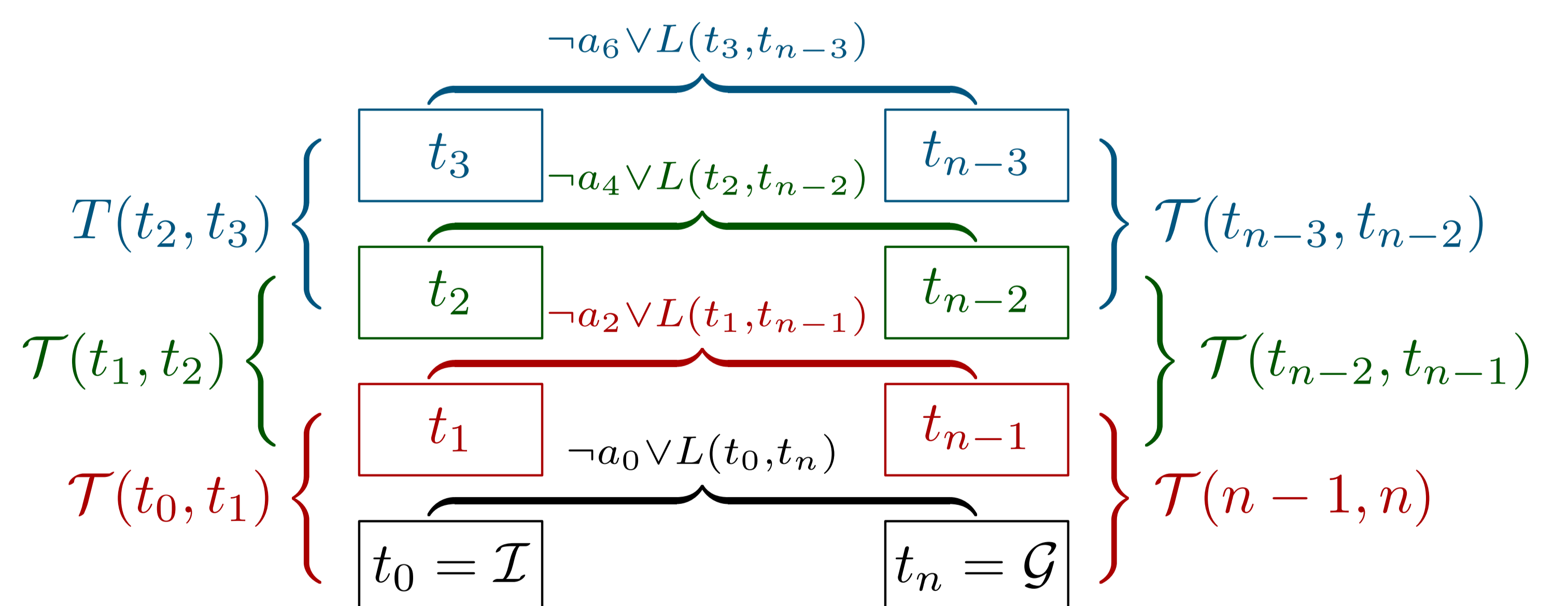
Cactusplot comparing madagascar with our approach.

4. Incremental SAT Solving

- Standardized interface IPASIR
 - profit from future SAT solver development
- Idea:** Solve multiple slightly different formulas
- Advantage:** Reuse information from previous solve:
 - Internally learned clauses
 - Importance of Variables and Clauses
 - Good assignments (phase saving)
 - ...
- Realization:**
 - Keep all added Clauses
 - Solve with assumptions (temporary unit clauses)
 - Allows de-/ activation of clauses via activation literals

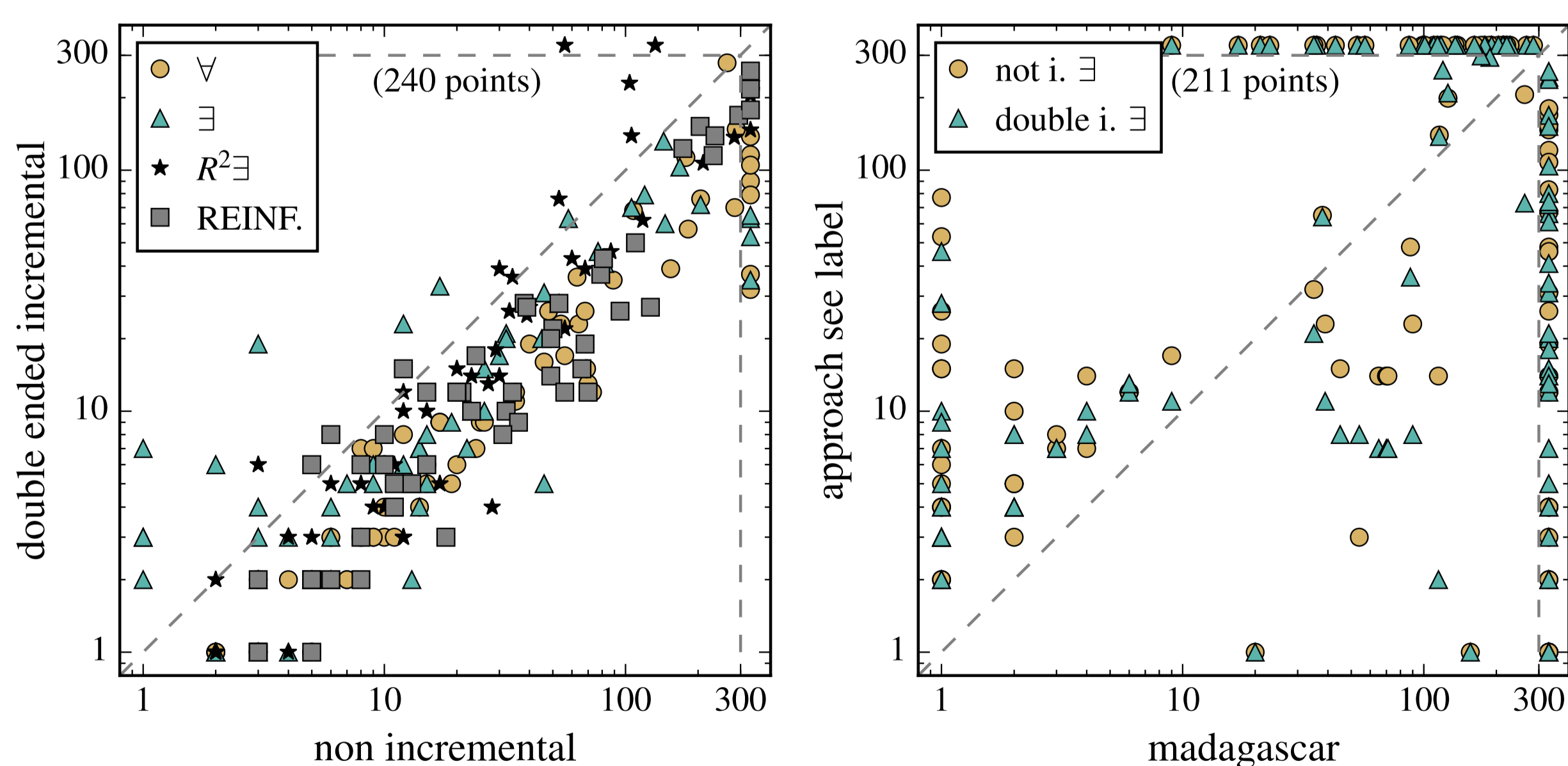
5. Extending F_n to F_{n+1}

- Add new timepoints with transitions alternating to goal and initial state.
- At step n the formula F_n is solved with assumption a_n and contains all clauses of previous steps.
- $L(t_i, t_j)$ is a link clauses such that all variables in t_i have the same value as in t_j and vice versa. As it has an activation literal, only the latest link clause is active.



■ step 0 ■ step 2 ■ step 4 ■ step 6

Double Ended Incremental Encoding up to step 6 and with step size 2.



The Scatter Plots show a data point for each problem. If a problem is only solved by one approach but not the other it is plotted behind the 300 second.

7. Conclusion

- Incremental SAT solving is very beneficial
- It is important to keep track of SAT solver development

6. Experiments

- Recent SAT solver from 2016 SAT Competition:
 - COMiniSatPS 2Sun nopre
- Benchmarks:
 - Agile Track of the 2014 International Planning Competition (IPC)
- Limits:
 - Time limit: 300s, 1 CPU core @ 2.10GHz, 8 GB RAM