

# Relaxing the Relaxed Exist-Step Parallel Planning Semantics



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# What is Planning?

- World states are described as values of state variables
- Actions change the state of the world by changing the values of state variables by their effects
- Actions also have preconditions and are applicable only when their preconditions hold in the given state

**Objective:** given a set  $a$  of actions, an initial world state and the description of a goal state find a valid sequence of actions that transforms the world from the initial state to a goal state





### State Variables and their domains:

- Truck location  $T$ ,  $\text{dom}(T) = \{LA, SF, LV\}$
  - Package locations  $P$  and  $Q$
- $\text{dom}(P) = \text{dom}(Q) = \{LA, SF, LV, Tr\}$

**Initial State:**  $T=LA, P=LA, Q=SF$

**Goal State:**  $P=LV, Q=LV$

### Actions:

- $\text{move}(x,y) = [\text{prec: } \{T=x\}, \text{eff: } \{T=y\}]$
- $\text{loadP}(x) = [\text{prec: } \{T=x, P=x\}, \text{eff: } \{P=Tr\}]$
- $\text{loadQ}(x) = [\text{prec: } \{T=x, Q=x\}, \text{eff: } \{Q=Tr\}]$
- $\text{dropP}(x) = [\text{prec: } \{T=x, P=Tr\}, \text{eff: } \{P=x\}]$
- $\text{dropQ}(x) = [\text{prec: } \{T=x, Q=Tr\}, \text{eff: } \{Q=x\}]$

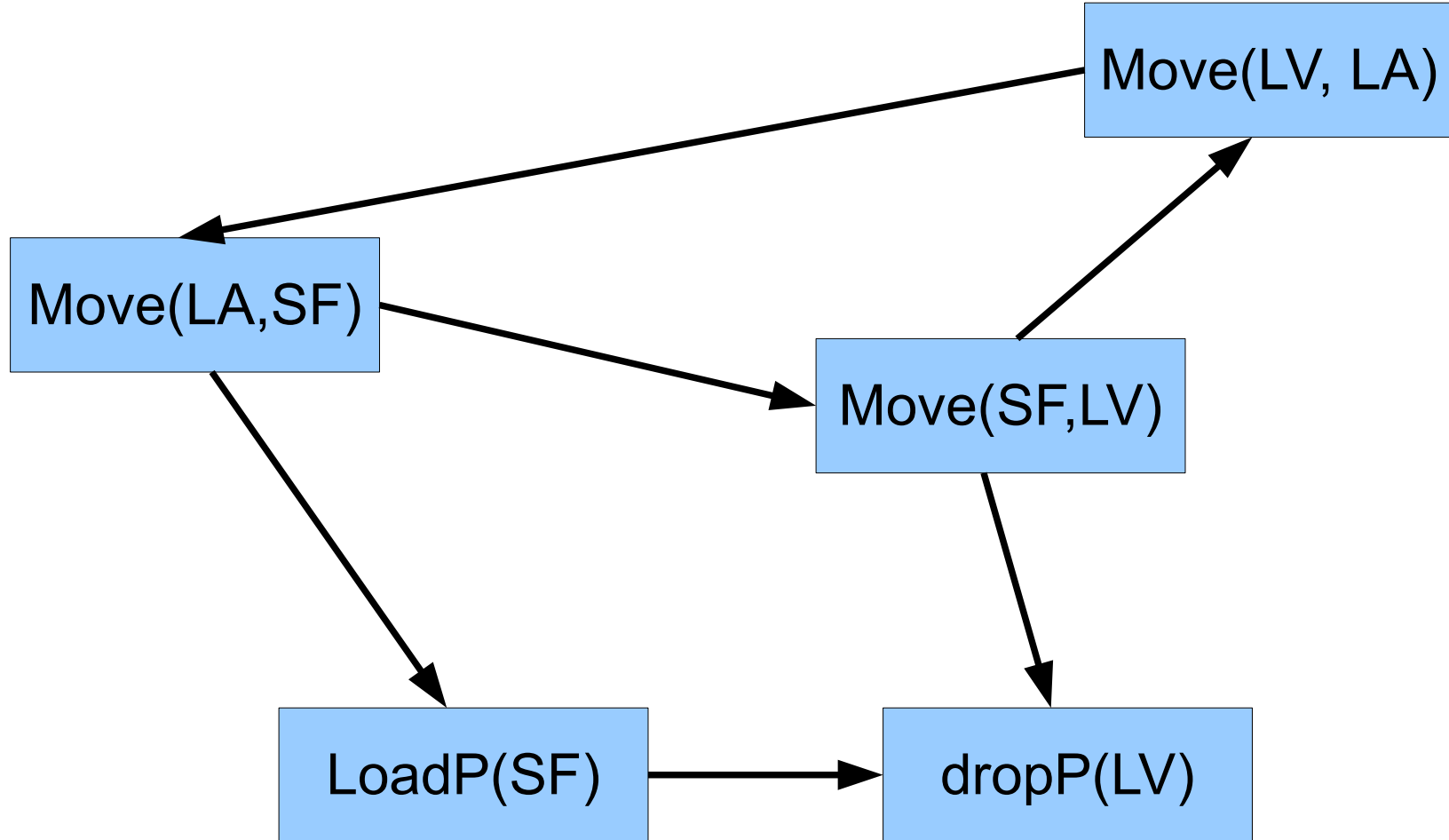
Where  $x, y$  are LA, SF, and LV

**Plan:**  $\text{loadP}(LA), \text{move}(LA, SF), \text{loadQ}(SF), \text{move}(SF, LV), \text{dropP}(LV), \text{dropQ}(LV)$

# Enabling Graph

$$V = \{ \text{Actions} \}$$

$$E = \{ (A_1 \rightarrow A_2), \text{eff}(A_1) \cap \text{prec}(A_2) \neq 0 \}$$



# Planning as SATisfiability

- Construct a formula  $F_k$  such that it is satisfiable (if and) only if there is a plan of at most  $k$  steps
- Solve  $F_1, F_2, \dots$  using a SAT solver until you reach a satisfiable formula  $F_n$
- Extract a plan from the satisfying assignment of  $F_n$
- $n$  is the called the makespan of the plan
- ***What actions can go inside a step together?***
  - If more action could be in a step then we would need fewer steps to find a plan

What actions can go inside a step together?

## 1. foreach step semantics

- The preconditions of all actions in a step must already hold in the beginning of the step
- The effects of all actions must hold at the end of this step
- The actions in a step do not interfere – they cannot destroy each others preconditions by their effects
- The actions in a step can be turned into a valid subplan sequence
- Plan: {loadP(LA)} ♦ {move(LA, SF)} ♦ {loadQ(SF)} ♦ {move(SF, LV)} ♦ {dropP(LV), dropQ(LV)} – **5 steps**

What actions can go inside a step together?

## 2. exist step semantics

- The preconditions of all actions in a step must already hold in the beginning of the step
- The effects of all actions must hold at the end of this step
- ~~The actions in a step do not interfere – they cannot destroy each others preconditions by their effects~~
- The actions in a step can be turned into a valid subplan sequence
- Plan: {loadP(LA), move(LA, SF)} ♦ {loadQ(SF), move(SF, LV)} ♦ {dropP(LV), dropQ(LV)} – **3 steps**

What actions can go inside a step together?

### 3. relaxed exist step semantics

- ~~The preconditions of all actions in a step must already hold in the beginning of the step~~
- The effects of all actions must hold at the end of this step
- ~~The actions in a step do not interfere — they cannot destroy each others preconditions by their effects~~
- The actions in a step can be turned into a valid subplan sequence
- Plan: {loadP(LA), move(LA, SF), loadQ(SF)} ♦ {move(SF, LV), dropP(LV), dropQ(LV)} – **2 steps**



What actions can go inside a step together?

## 4. relaxed relaxed exist step semantics

- ~~The preconditions of all actions in a step must already hold in the beginning of the step~~
- ~~The effects of all actions must hold at the end of this step~~
- ~~The actions in a step do not interfere — they cannot destroy each others preconditions by their effects~~
- The actions in a step can be turned into a valid subplan sequence
- Plan: {loadP(LA), move(LA, SF), loadQ(SF), move(SF, LV), dropP(LV), dropQ(LV)} – **1 step**

# Basic ideas of the relaxed relaxed exist step SAT encoding

- The SAT encoding only approximates the semantics, i.e., the satisfiability of the constructed formula  $F_k$  implies the existence of a k-step plan (not vice versa)
- The actions are ranked using cycle-ignoring topological sorting on the enabling graph (action ranking can be arbitrary as long as it is injective)
- The encoding allows only lower ranking actions before higher ranking ones in a step
- The encoding uses implication chains similar to those used in the exist step and relaxed exist step encoding

# Experimental Results

- IPC 2012 domains (20 problems each), time limit 30 minutes

Domain	Foreach Step		Exist Step		Relaxed Relaxed E.S.	
	Solved	Avg. Steps	Solved	Avg. Steps	Solved	Avg. Steps
Barman	8	46.3	8	36.6	14	14.8
Elevators	20	9.5	20	6.5	20	4.3
Parcprinter	20	13.5	20	13.5	20	1.5
Pegsol	7	22.8	13	24.0	19	8.6
Storage	15	9.2	19	7.9	19	4.3
Visitall	9	27.0	11	31.4	20	1.7
Woodwork	20	3.4	20	3.3	20	1.7
Zenotravel	16	5.9	16	4.5	15	2.7

# Conclusion

- We have defined a novel parallel planning semantics and a SAT encoding which approximates it
- The results of the experiments show that the new encoding is successful in solving IPC benchmark problems
- For the domains Pegsol, Barman, and Visitall we achieved a significant improvement in the number of solved instances
- The average number of required steps decreased for all domains, most significantly for the Visitall domain
- The encoding can be further improved to produce smaller formulas and to better approximate the defined semantics